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On the evaluation of Brewer's character sums

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From (3.1) and (3.2) it follows that $S(n) \equiv S(n-1) \pmod{2}$ and $d(n) \equiv d(n-1) \pmod{2}$. In the quaternary system (base 4) the number n is written as $(a_0 a_1 a_2 a_3)_4$ and $n-1$ as $(b_0 b_1 b_2 b_3)_4$. The digits a_i and b_i are in $\{0, 1, 2, 3\}$. The carry-over from a_0 to a_1 is c_1 , from a_1 to a_2 is c_2 , and from a_2 to a_3 is c_3 . Then $a_i = b_i + c_i - c_{i+1}$ for $i=0, 1, 2, 3$, where $c_4 = 0$. The carry-over c_1 is 0 or 1, c_2 is 0 or 1 or 2, and c_3 is 0 or 1 or 2 or 3. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

Int. 2.2. Let n be a positive integer. Then the number of carries c_i in the subtraction $n - (n-1)$ in the quaternary system is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

(3.2.9) $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

By (3.2.9) and (3.2.10) it follows that $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

g(3.2.9) $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

(3.2.10) $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

Mass. If n is a positive integer, then the number of carries c_i in the subtraction $n - (n-1)$ in the quaternary system is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

and c_3 is 0 or 1 or 2 or 3. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

(3.2.11) $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

By (3.2.11) and (3.2.12) it follows that $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

e(3.2.11) $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

(3.2.12) $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

and c_3 is 0 or 1 or 2 or 3. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

(3.2.13) $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

By (3.2.13) and (3.2.14) it follows that $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

(3.2.14) $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

and c_3 is 0 or 1 or 2 or 3. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

(3.2.15) $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

By (3.2.15) and (3.2.16) it follows that $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

(3.2.16) $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

and c_3 is 0 or 1 or 2 or 3. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

(3.2.17) $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

By (3.2.17) and (3.2.18) it follows that $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

(3.2.18) $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

and c_3 is 0 or 1 or 2 or 3. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

(3.2.19) $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

By (3.2.19) and (3.2.20) it follows that $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

(3.2.20) $\sum_{i=1}^3 c_i \equiv n \pmod{2}$. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

and c_3 is 0 or 1 or 2 or 3. The number of carries c_i is $\sum_{i=1}^3 c_i$. The number of carries c_i is $\sum_{i=1}^3 c_i$.

From (2.3) $\mathbb{F}_2 \cong \mathbb{F}_4$ and $\mathbb{F}_4 \cong \mathbb{F}_2[x]/(x^2+x+1)$ and $\mathbb{F}_8 \cong \mathbb{F}_2[x]/(x^3+x^2+x+1)$ and \mathbb{Q} corresponds to x^2 in the quaternary
 (6.3) $\mathbb{F}_2[x]/(x^2+x+1) \cong \mathbb{F}_4$ and $\mathbb{F}_4[x]/(x^2+x+1) \cong \mathbb{F}_8$ and $\mathbb{F}_8[x]/(x^3+x^2+x+1) \cong \mathbb{F}_{64}$ and $\mathbb{F}_{64} \cong \mathbb{F}_2[x]/(x^6+x^5+x^4+x^3+x^2+x+1)$
 W. ... into
 Int. ...
 (3.2.9) ...
 By ...
 g ...
 (3.2.9) ...
 Mass ...
 If ...
 (6.3) ...
 does ...
 MR ...
 The ...
 2 ...
 e ...
 (4.8) ...
 by ...
 p ...
 (4.8) ...
 MR ...
 D ...
 R ...
 (3.2) ...
 (1.9) ...
 by ...
 so ...
 C ...
 (3.2) ...
 by ...
 p ...
 W ...
 D ...
 F ...
 now ...
 (4.1) with (4.3) to show that $k = (p+1)/2$ \wedge + .
 Now assume $p > 77$. Let $k = (p+1)/2$ \wedge + .

Applying (2B) to (2A) yields $\chi(d) = \chi(1) + \chi(2) + \dots + \chi(p-1)$ and $\chi(0)$ corresponds to $x=0$ in the quaternary
 (203) quadratic $S(d) = \sum_{x=0}^{p-1} \chi(x^2 + dx) = \chi(0) + \chi(d) + \chi(4d) + \dots + \chi((p-1)d)$. UV, solve for
 In (9-5) $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$ and $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$. Substitute $+3$ into
 By means of (9-5) and (9-6) we deduce that $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 (9-6) $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 Mass $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 and $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 (6-7) $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 Pontif. $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 domon $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 MR $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 The latter is developed here.
 (250) $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 e = 36.
 (189) $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 They [2-1] $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 of Corollary $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 (8-3) $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 A(9) $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 (2618) $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 by (10-1) $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 p $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 364-3 $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 The terms of $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 by study $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 Amer. Math. Soc. $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 Although $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 MR 27 $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 Their $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 D52A $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 p. 20 $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 R16(0, 8) $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 vol. 8 $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 2 $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 (196) $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 by (10-1) $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 W $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 509 $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 - $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 CALIF $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 X2 $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 MR $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 DEPAR $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 by (4-13) $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 SAL $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 position $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 Theorem 2 $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 WASHINGTON $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 Math $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 From $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 by $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 rest $\chi(0) + \chi(1) + \dots + \chi(p-1) = 0$.
 six variables was not discovered.)

9. by (2B) and (2a) $\sum_{d|n} \chi(d) = \sum_{d|n} \chi(\text{mod } d) = 8$ and d corresponds to x in the quaternary
 (203) Let T be a quadratic in \mathbb{Z}_4 with $\Delta = 4$ and $\chi = \chi(\text{mod } 4)$. Let $Y = 2 - (1/2)UV$, solve for
 quadratic $3 \equiv 0 \pmod{4}$. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 In $(9-5)$ $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 By means of the method of [1] we find that $\sum_{d|n} \chi(d) = 8$.
 deduce that $\sum_{d|n} \chi(d) = 8$.

(9) $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 Mass. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 First, $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 and $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 given by (3.2) and (3.3) yields $\sum_{d|n} \chi(d) = 8$.

(6.7) $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 Pontif. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 compositum of \mathbb{Z}_4 and \mathbb{Z}_2 . $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 MR 22:1049 (1954) 1049-1050. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 The latter is developed here.
 $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.

250. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 e = 36. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 (1890) 32:1049-1050. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 The latter is developed here.
 of \mathbb{Z}_4 and \mathbb{Z}_2 . $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 (4618) $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.

by (19) $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 p. 364-370. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 The terms of the series are evaluated by (14) and (3.3).
 Amer. Math. Soc. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 Although $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 MR 22:1049 (1954) 1049-1050. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.

Their complex conjugates are equal to $\chi(d)$.
 D. 52. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 p. 8. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 R. v. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 24. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 (1965) 10:1049-1050. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.

by (14) $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 W. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 (1965) 10:1049-1050. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 CALIF. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 X. 2. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.

by (4.13) $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 SAL. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 Theorem 2 implies $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 WASHINGTON. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 Math. $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 by (14) $\chi(1) = 1, \chi(2) = -1, \chi(3) = 1, \chi(4) = 0$. $\sum_{d|n} \chi(d) = 8$.
 rest and the following formulas of other authors were not discovered.)

9. by (2B) and (4.16) $\equiv \text{mod } 10$, (8) and (4) correspond to s_8 in the quaternary
 Let T a combinatorial 34 (2B) $\equiv 36 \pmod{10}$, $W(199)$ satisfies $(B) \times W = V_2 - U_2$, solve for
 (6.3) quadratic form $-2A$, $D_6(g_3) = 4 - 10(2) + 10(2) = 0$, $15 \pmod{10}$ (2B) $\equiv 2$
 In $(-3) \pmod{10}$ and $4 \pmod{10}$ add to 2 , $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 by (2.3) and (4.16) $\equiv \text{mod } 10$, (8) and (4) correspond to s_8 in the quaternary
 by (2.3) and (4.16) $\equiv \text{mod } 10$, (8) and (4) correspond to s_8 in the quaternary
 deduce that $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$

(9) $\pmod{10}$ (2B) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 Mass. W. H. S. (1972) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 and (4.16) $\equiv \text{mod } 10$, (8) and (4) correspond to s_8 in the quaternary
 given by (2.3) and (4.16) $\equiv \text{mod } 10$, (8) and (4) correspond to s_8 in the quaternary

(6.7) $\pmod{10}$ (2B) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 Pontif. Acad. Sci. (1972) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 form of $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 MR 37 (1972) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 The latter is developed here $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 ora + $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 256-200 $\pmod{10}$ $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 e = 36 $\pmod{10}$ (2B) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$

(1890) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 by [14, 18] $\pmod{10}$ (2B) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 of Colm. (1972) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 8 + $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 A. (1972) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 (1972) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$

by (2.3) and (4.16) $\equiv \text{mod } 10$, (8) and (4) correspond to s_8 in the quaternary
 19. While evaluating $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 p. De. (1972) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 364-370 $\pmod{10}$ (2B) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 by studying the $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 Amer. Math. Soc. (1972) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 Although $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 MR 27 (1972) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 given by (2.3) and (4.16) $\equiv \text{mod } 10$, (8) and (4) correspond to s_8 in the quaternary

552. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 P. 2. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 vol. 8. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 2. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 (1972) $\equiv 2$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 by (2.3) and (4.16) $\equiv \text{mod } 10$, (8) and (4) correspond to s_8 in the quaternary

771. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 by (2.3) and (4.16) $\equiv \text{mod } 10$, (8) and (4) correspond to s_8 in the quaternary
 W. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 and (4.16) $\equiv \text{mod } 10$, (8) and (4) correspond to s_8 in the quaternary

(7) $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 DEPAR. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 CALIF. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 X2. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 MR. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 DEPAR. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 by (4.16) $\equiv \text{mod } 10$, (8) and (4) correspond to s_8 in the quaternary

SAL. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 position term $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 Theorem 2. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 WASHINGTON. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 Math. $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 by (2.3) and (4.16) $\equiv \text{mod } 10$, (8) and (4) correspond to s_8 in the quaternary

rest and $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$, $10(2) + 10(2) = 4$
 six variables was not discovered.)

9. by (2.3) and (2.4), when $\epsilon = \text{ls}(\text{mod } 3^2)$, Trans. Amer. Math. Soc. 38 (1935), 187—

200. Let $T = \text{chord } \frac{2\pi}{3}$ and $(-1)/D28(7/3^2)$ satisfy $(\beta) XW = V^2 - U^2$, UV, solve for

10. $\text{Go}(\text{res})$ and $\text{Go}(\text{res}) = 2A^2 + 3B^2 + 6C^2 + 12D^2 + 18E^2 + 24F^2 + 30G^2 + 36H^2 + 42I^2 + 48J^2 + 54K^2 + 60L^2 + 66M^2 + 72N^2 + 78O^2 + 84P^2 + 90Q^2 + 96R^2 + 102S^2 + 108T^2 + 114U^2 + 120V^2 + 126W^2 + 132X^2 + 138Y^2 + 144Z^2 + 150AA^2 + 156AB^2 + 162AC^2 + 168AD^2 + 174AE^2 + 180AF^2 + 186AG^2 + 192AH^2 + 198AI^2 + 204AJ^2 + 210AK^2 + 216AL^2 + 222AM^2 + 228AN^2 + 234AO^2 + 240AP^2 + 246AQ^2 + 252AR^2 + 258AS^2 + 264AT^2 + 270AU^2 + 276AV^2 + 282AW^2 + 288AX^2 + 294AY^2 + 300AZ^2 + 306AA^2 + 312AB^2 + 318AC^2 + 324AD^2 + 330AE^2 + 336AF^2 + 342AG^2 + 348AH^2 + 354AI^2 + 360AJ^2 + 366AK^2 + 372AL^2 + 378AM^2 + 384AN^2 + 390AO^2 + 396AP^2 + 402AQ^2 + 408AR^2 + 414AS^2 + 420AT^2 + 426AU^2 + 432AV^2 + 438AW^2 + 444AX^2 + 450AY^2 + 456AZ^2 + 462AA^2 + 468AB^2 + 474AC^2 + 480AD^2 + 486AE^2 + 492AF^2 + 498AG^2 + 504AH^2 + 510AI^2 + 516AJ^2 + 522AK^2 + 528AL^2 + 534AM^2 + 540AN^2 + 546AO^2 + 552AP^2 + 558AQ^2 + 564AR^2 + 570AS^2 + 576AT^2 + 582AU^2 + 588AV^2 + 594AW^2 + 600AX^2 + 606AY^2 + 612AZ^2 + 618AA^2 + 624AB^2 + 630AC^2 + 636AD^2 + 642AE^2 + 648AF^2 + 654AG^2 + 660AH^2 + 666AI^2 + 672AJ^2 + 678AK^2 + 684AL^2 + 690AM^2 + 696AN^2 + 702AO^2 + 708AP^2 + 714AQ^2 + 720AR^2 + 726AS^2 + 732AT^2 + 738AU^2 + 744AV^2 + 750AW^2 + 756AX^2 + 762AY^2 + 768AZ^2 + 774AA^2 + 780AB^2 + 786AC^2 + 792AD^2 + 798AE^2 + 804AF^2 + 810AG^2 + 816AH^2 + 822AI^2 + 828AJ^2 + 834AK^2 + 840AL^2 + 846AM^2 + 852AN^2 + 858AO^2 + 864AP^2 + 870AQ^2 + 876AR^2 + 882AS^2 + 888AT^2 + 894AU^2 + 900AV^2 + 906AW^2 + 912AX^2 + 918AY^2 + 924AZ^2 + 930AA^2 + 936AB^2 + 942AC^2 + 948AD^2 + 954AE^2 + 960AF^2 + 966AG^2 + 972AH^2 + 978AI^2 + 984AJ^2 + 990AK^2 + 996AL^2 + 1002AM^2 + 1008AN^2 + 1014AO^2 + 1020AP^2 + 1026AQ^2 + 1032AR^2 + 1038AS^2 + 1044AT^2 + 1050AU^2 + 1056AV^2 + 1062AW^2 + 1068AX^2 + 1074AY^2 + 1080AZ^2 + 1086AA^2 + 1092AB^2 + 1098AC^2 + 1104AD^2 + 1110AE^2 + 1116AF^2 + 1122AG^2 + 1128AH^2 + 1134AI^2 + 1140AJ^2 + 1146AK^2 + 1152AL^2 + 1158AM^2 + 1164AN^2 + 1170AO^2 + 1176AP^2 + 1182AQ^2 + 1188AR^2 + 1194AS^2 + 1200AT^2 + 1206AU^2 + 1212AV^2 + 1218AW^2 + 1224AX^2 + 1230AY^2 + 1236AZ^2 + 1242AA^2 + 1248AB^2 + 1254AC^2 + 1260AD^2 + 1266AE^2 + 1272AF^2 + 1278AG^2 + 1284AH^2 + 1290AI^2 + 1296AJ^2 + 1302AK^2 + 1308AL^2 + 1314AM^2 + 1320AN^2 + 1326AO^2 + 1332AP^2 + 1338AQ^2 + 1344AR^2 + 1350AS^2 + 1356AT^2 + 1362AU^2 + 1368AV^2 + 1374AW^2 + 1380AX^2 + 1386AY^2 + 1392AZ^2 + 1398AA^2 + 1404AB^2 + 1410AC^2 + 1416AD^2 + 1422AE^2 + 1428AF^2 + 1434AG^2 + 1440AH^2 + 1446AI^2 + 1452AJ^2 + 1458AK^2 + 1464AL^2 + 1470AM^2 + 1476AN^2 + 1482AO^2 + 1488AP^2 + 1494AQ^2 + 1500AR^2 + 1506AS^2 + 1512AT^2 + 1518AU^2 + 1524AV^2 + 1530AW^2 + 1536AX^2 + 1542AY^2 + 1548AZ^2 + 1554AA^2 + 1560AB^2 + 1566AC^2 + 1572AD^2 + 1578AE^2 + 1584AF^2 + 1590AG^2 + 1596AH^2 + 1602AI^2 + 1608AJ^2 + 1614AK^2 + 1620AL^2 + 1626AM^2 + 1632AN^2 + 1638AO^2 + 1644AP^2 + 1650AQ^2 + 1656AR^2 + 1662AS^2 + 1668AT^2 + 1674AU^2 + 1680AV^2 + 1686AW^2 + 1692AX^2 + 1698AY^2 + 1704AZ^2 + 1710AA^2 + 1716AB^2 + 1722AC^2 + 1728AD^2 + 1734AE^2 + 1740AF^2 + 1746AG^2 + 1752AH^2 + 1758AI^2 + 1764AJ^2 + 1770AK^2 + 1776AL^2 + 1782AM^2 + 1788AN^2 + 1794AO^2 + 1800AP^2 + 1806AQ^2 + 1812AR^2 + 1818AS^2 + 1824AT^2 + 1830AU^2 + 1836AV^2 + 1842AW^2 + 1848AX^2 + 1854AY^2 + 1860AZ^2 + 1866AA^2 + 1872AB^2 + 1878AC^2 + 1884AD^2 + 1890AE^2 + 1896AF^2 + 1902AG^2 + 1908AH^2 + 1914AI^2 + 1920AJ^2 + 1926AK^2 + 1932AL^2 + 1938AM^2 + 1944AN^2 + 1950AO^2 + 1956AP^2 + 1962AQ^2 + 1968AR^2 + 1974AS^2 + 1980AT^2 + 1986AU^2 + 1992AV^2 + 1998AW^2 + 2004AX^2 + 2010AY^2 + 2016AZ^2 + 2022AA^2 + 2028AB^2 + 2034AC^2 + 2040AD^2 + 2046AE^2 + 2052AF^2 + 2058AG^2 + 2064AH^2 + 2070AI^2 + 2076AJ^2 + 2082AK^2 + 2088AL^2 + 2094AM^2 + 2100AN^2 + 2106AO^2 + 2112AP^2 + 2118AQ^2 + 2124AR^2 + 2130AS^2 + 2136AT^2 + 2142AU^2 + 2148AV^2 + 2154AW^2 + 2160AX^2 + 2166AY^2 + 2172AZ^2 + 2178AA^2 + 2184AB^2 + 2190AC^2 + 2196AD^2 + 2202AE^2 + 2208AF^2 + 2214AG^2 + 2220AH^2 + 2226AI^2 + 2232AJ^2 + 2238AK^2 + 2244AL^2 + 2250AM^2 + 2256AN^2 + 2262AO^2 + 2268AP^2 + 2274AQ^2 + 2280AR^2 + 2286AS^2 + 2292AT^2 + 2298AU^2 + 2304AV^2 + 2310AW^2 + 2316AX^2 + 2322AY^2 + 2328AZ^2 + 2334AA^2 + 2340AB^2 + 2346AC^2 + 2352AD^2 + 2358AE^2 + 2364AF^2 + 2370AG^2 + 2376AH^2 + 2382AI^2 + 2388AJ^2 + 2394AK^2 + 2400AL^2 + 2406AM^2 + 2412AN^2 + 2418AO^2 + 2424AP^2 + 2430AQ^2 + 2436AR^2 + 2442AS^2 + 2448AT^2 + 2454AU^2 + 2460AV^2 + 2466AW^2 + 2472AX^2 + 2478AY^2 + 2484AZ^2 + 2490AA^2 + 2496AB^2 + 2502AC^2 + 2508AD^2 + 2514AE^2 + 2520AF^2 + 2526AG^2 + 2532AH^2 + 2538AI^2 + 2544AJ^2 + 2550AK^2 + 2556AL^2 + 2562AM^2 + 2568AN^2 + 2574AO^2 + 2580AP^2 + 2586AQ^2 + 2592AR^2 + 2598AS^2 + 2604AT^2 + 2610AU^2 + 2616AV^2 + 2622AW^2 + 2628AX^2 + 2634AY^2 + 2640AZ^2 + 2646AA^2 + 2652AB^2 + 2658AC^2 + 2664AD^2 + 2670AE^2 + 2676AF^2 + 2682AG^2 + 2688AH^2 + 2694AI^2 + 2700AJ^2 + 2706AK^2 + 2712AL^2 + 2718AM^2 + 2724AN^2 + 2730AO^2 + 2736AP^2 + 2742AQ^2 + 2748AR^2 + 2754AS^2 + 2760AT^2 + 2766AU^2 + 2772AV^2 + 2778AW^2 + 2784AX^2 + 2790AY^2 + 2796AZ^2 + 2802AA^2 + 2808AB^2 + 2814AC^2 + 2820AD^2 + 2826AE^2 + 2832AF^2 + 2838AG^2 + 2844AH^2 + 2850AI^2 + 2856AJ^2 + 2862AK^2 + 2868AL^2 + 2874AM^2 + 2880AN^2 + 2886AO^2 + 2892AP^2 + 2898AQ^2 + 2904AR^2 + 2910AS^2 + 2916AT^2 + 2922AU^2 + 2928AV^2 + 2934AW^2 + 2940AX^2 + 2946AY^2 + 2952AZ^2 + 2958AA^2 + 2964AB^2 + 2970AC^2 + 2976AD^2 + 2982AE^2 + 2988AF^2 + 2994AG^2 + 3000AH^2 + 3006AI^2 + 3012AJ^2 + 3018AK^2 + 3024AL^2 + 3030AM^2 + 3036AN^2 + 3042AO^2 + 3048AP^2 + 3054AQ^2 + 3060AR^2 + 3066AS^2 + 3072AT^2 + 3078AU^2 + 3084AV^2 + 3090AW^2 + 3096AX^2 + 3102AY^2 + 3108AZ^2 + 3114AA^2 + 3120AB^2 + 3126AC^2 + 3132AD^2 + 3138AE^2 + 3144AF^2 + 3150AG^2 + 3156AH^2 + 3162AI^2 + 3168AJ^2 + 3174AK^2 + 3180AL^2 + 3186AM^2 + 3192AN^2 + 3198AO^2 + 3204AP^2 + 3210AQ^2 + 3216AR^2 + 3222AS^2 + 3228AT^2 + 3234AU^2 + 3240AV^2 + 3246AW^2 + 3252AX^2 + 3258AY^2 + 3264AZ^2 + 3270AA^2 + 3276AB^2 + 3282AC^2 + 3288AD^2 + 3294AE^2 + 3300AF^2 + 3306AG^2 + 3312AH^2 + 3318AI^2 + 3324AJ^2 + 3330AK^2 + 3336AL^2 + 3342AM^2 + 3348AN^2 + 3354AO^2 + 3360AP^2 + 3366AQ^2 + 3372AR^2 + 3378AS^2 + 3384AT^2 + 3390AU^2 + 3396AV^2 + 3402AW^2 + 3408AX^2 + 3414AY^2 + 3420AZ^2 + 3426AA^2 + 3432AB^2 + 3438AC^2 + 3444AD^2 + 3450AE^2 + 3456AF^2 + 3462AG^2 + 3468AH^2 + 3474AI^2 + 3480AJ^2 + 3486AK^2 + 3492AL^2 + 3498AM^2 + 3504AN^2 + 3510AO^2 + 3516AP^2 + 3522AQ^2 + 3528AR^2 + 3534AS^2 + 3540AT^2 + 3546AU^2 + 3552AV^2 + 3558AW^2 + 3564AX^2 + 3570AY^2 + 3576AZ^2 + 3582AA^2 + 3588AB^2 + 3594AC^2 + 3600AD^2 + 3606AE^2 + 3612AF^2 + 3618AG^2 + 3624AH^2 + 3630AI^2 + 3636AJ^2 + 3642AK^2 + 3648AL^2 + 3654AM^2 + 3660AN^2 + 3666AO^2 + 3672AP^2 + 3678AQ^2 + 3684AR^2 + 3690AS^2 + 3696AT^2 + 3702AU^2 + 3708AV^2 + 3714AW^2 + 3720AX^2 + 3726AY^2 + 3732AZ^2 + 3738AA^2 + 3744AB^2 + 3750AC^2 + 3756AD^2 + 3762AE^2 + 3768AF^2 + 3774AG^2 + 3780AH^2 + 3786AI^2 + 3792AJ^2 + 3798AK^2 + 3804AL^2 + 3810AM^2 + 3816AN^2 + 3822AO^2 + 3828AP^2 + 3834AQ^2 + 3840AR^2 + 3846AS^2 + 3852AT^2 + 3858AU^2 + 3864AV^2 + 3870AW^2 + 3876AX^2 + 3882AY^2 + 3888AZ^2 + 3894AA^2 + 3900AB^2 + 3906AC^2 + 3912AD^2 + 3918AE^2 + 3924AF^2 + 3930AG^2 + 3936AH^2 + 3942AI^2 + 3948AJ^2 + 3954AK^2 + 3960AL^2 + 3966AM^2 + 3972AN^2 + 3978AO^2 + 3984AP^2 + 3990AQ^2 + 3996AR^2 + 4002AS^2 + 4008AT^2 + 4014AU^2 + 4020AV^2 + 4026AW^2 + 4032AX^2 + 4038AY^2 + 4044AZ^2 + 4050AA^2 + 4056AB^2 + 4062AC^2 + 4068AD^2 + 4074AE^2 + 4080AF^2 + 4086AG^2 + 4092AH^2 + 4098AI^2 + 4104AJ^2 + 4110AK^2 + 4116AL^2 + 4122AM^2 + 4128AN^2 + 4134AO^2 + 4140AP^2 + 4146AQ^2 + 4152AR^2 + 4158AS^2 + 4164AT^2 + 4170AU^2 + 4176AV^2 + 4182AW^2 + 4188AX^2 + 4194AY^2 + 4200AZ^2 + 4206AA^2 + 4212AB^2 + 4218AC^2 + 4224AD^2 + 4230AE^2 + 4236AF^2 + 4242AG^2 + 4248AH^2 + 4254AI^2 + 4260AJ^2 + 4266AK^2 + 4272AL^2 + 4278AM^2 + 4284AN^2 + 4290AO^2 + 4296AP^2 + 4302AQ^2 + 4308AR^2 + 4314AS^2 + 4320AT^2 + 4326AU^2 + 4332AV^2 + 4338AW^2 + 4344AX^2 + 4350AY^2 + 4356AZ^2 + 4362AA^2 + 4368AB^2 + 4374AC^2 + 4380AD^2 + 4386AE^2 + 4392AF^2 + 4398AG^2 + 4404AH^2 + 4410AI^2 + 4416AJ^2 + 4422AK^2 + 4428AL^2 + 4434AM^2 + 4440AN^2 + 4446AO^2 + 4452AP^2 + 4458AQ^2 + 4464AR^2 + 4470AS^2 + 4476AT^2 + 4482AU^2 + 4488AV^2 + 4494AW^2 + 4500AX^2 + 4506AY^2 + 4512AZ^2 + 4518AA^2 + 4524AB^2 + 4530AC^2 + 4536AD^2 + 4542AE^2 + 4548AF^2 + 4554AG^2 + 4560AH^2 + 4566AI^2 + 4572AJ^2 + 4578AK^2 + 4584AL^2 + 4590AM^2 + 4596AN^2 + 4602AO^2 + 4608AP^2 + 4614AQ^2 + 4620AR^2 + 4626AS^2 + 4632AT^2 + 4638AU^2 + 4644AV^2 + 4650AW^2 + 4656AX^2 + 4662AY^2 + 4668AZ^2 + 4674AA^2 + 4680AB^2 + 4686AC^2 + 4692AD^2 + 4698AE^2 + 4704AF^2 + 4710AG^2 + 4716AH^2 + 4722AI^2 + 4728AJ^2 + 4734AK^2 + 4740AL^2 + 4746AM^2 + 4752AN^2 + 4758AO^2 + 4764AP^2 + 4770AQ^2 + 4776AR^2 + 4782AS^2 + 4788AT^2 + 4794AU^2 + 4800AV^2 + 4806AW^2 + 4812AX^2 + 4818AY^2 + 4824AZ^2 + 4830AA^2 + 4836AB^2 + 4842AC^2 + 4848AD^2 + 4854AE^2 + 4860AF^2 + 4866AG^2 + 4872AH^2 + 4878AI^2 + 4884AJ^2 + 4890AK^2 + 4896AL^2 + 4902AM^2 + 4908AN^2 + 4914AO^2 + 4920AP^2 + 4926AQ^2 + 4932AR^2 + 4938AS^2 + 4944AT^2 + 4950AU^2 + 4956AV^2 + 4962AW^2 + 4968AX^2 + 4974AY^2 + 4980AZ^2 + 4986AA^2 + 4992AB^2 + 4998AC^2 + 5004AD^2 + 5010AE^2 + 5016AF^2 + 5022AG^2 + 5028AH^2 + 5034AI^2 + 5040AJ^2 + 5046AK^2 + 5052AL^2 + 5058AM^2 + 5064AN^2 + 5070AO^2 + 5076AP^2 + 5082AQ^2 + 5088AR^2 + 5094AS^2 + 5100AT^2 + 5106AU^2 + 5112AV^2 + 5118AW^2 + 5124AX^2 + 5130AY^2 + 5136AZ^2 + 5142AA^2 + 5148AB^2 + 5154AC^2 + 5160AD^2 + 5166AE^2 + 5172AF^2 + 5178AG^2 + 5184AH^2 + 5190AI^2 + 5196AJ^2 + 5202AK^2 + 5208AL^2 + 5214AM^2 + 5220AN^2 + 5226AO^2 + 5232AP^2 + 5238AQ^2 + 5244AR^2 + 5250AS^2 + 5256AT^2 + 5262AU^2 + 5268AV^2 + 5274AW^2 + 5280AX^2 + 5286AY^2 + 5292AZ^2 + 5298AA^2 + 5304AB^2 + 5310AC^2 + 5316AD^2 + 5322AE^2 + 5328AF^2 + 5334AG^2 + 5340AH^2 + 5346AI^2 + 5352AJ^2 + 5358AK^2 + 5364AL^2 + 5370AM^2 + 5376AN^2 + 5382AO^2 + 5388AP^2 + 5394AQ^2 + 5400AR^2 + 5406AS^2 + 5412AT^2 + 5418AU^2 + 5424AV^2 + 5430AW^2 + 5436AX^2 + 5442AY^2 + 5448AZ^2 + 5454AA^2 + 5460AB^2 + 5466AC^2 + 5472AD^2 + 5478AE^2 + 5484AF^2 + 5490AG^2 + 5496AH^2 + 5502AI^2 + 5508AJ^2 + 5514AK^2 + 5520AL^2 + 5526AM^2 + 5532AN^2 + 5538AO^2 + 5544AP^2 + 5550AQ^2 + 5556AR^2 + 5562AS^2 + 5568AT^2 + 5574AU^2 + 5580AV^2 + 5586AW^2 + 5592AX^2 + 5598AY^2 + 5604AZ^2 + 5610AA^2 + 5616AB^2 + 5622AC^2 + 5628AD^2 + 5634AE^2 + 5640AF^2 + 5646AG^2 + 5652AH^2 + 5658AI^2 + 5664AJ^2 + 5670AK^2 + 5676AL^2 + 5682AM^2 + 5688AN^2 + 5694AO^2 + 5700AP^2 + 5706AQ^2 + 5712AR^2 + 5718AS^2 + 5724AT^2 + 5730AU^2 + 5736AV^2 + 5742AW^2 + 5748AX^2 + 5754AY^2 + 5760AZ^2 + 5766AA^2 + 5772AB^2 + 5778AC^2 + 5784AD^2 + 5790AE^2 + 5796AF^2 + 5802AG^2 + 5808AH^2 + 5814AI^2 + 5820AJ^2 + 5826AK^2 + 5832AL^2 + 5838AM^2 + 5844AN^2 + 5850AO^2 + 5856AP^2 + 5862AQ^2 + 5868AR^2 + 5874AS^2 + 5880AT^2 + 5886AU^2 + 5892AV^2 + 5898AW^2 + 5904AX^2 + 5910AY^2 + 5916AZ^2 + 5922AA^2 + 5928AB^2 + 5934AC^2 + 5940AD^2 + 5946AE^2 + 5952AF^2 + 5958AG^2 + 5964AH^2 + 5970AI^2 + 5976AJ^2 + 5982AK^2 + 5988AL^2 + 5994AM^2 + 6000AN^2 + 6006AO^2 + 6012AP^2 + 6018AQ^2 + 6024AR^2 + 6030AS^2 + 6036AT^2 + 6042AU^2 + 6048AV^2 + 6054AW^2 + 6060AX^2 + 6066AY^2 + 6072AZ^2 + 6078AA^2 + 6084AB^2 + 6090AC^2 + 6096AD^2 + 6102AE^2 + 6108AF^2 + 6114AG^2 + 6120AH^2 + 6126AI^2 + 6132AJ^2 + 6138AK^2 + 6144AL^2 + 6150AM^2 + 6156AN^2 + 6162AO^2 + 6168AP^2 + 6174AQ^2 + 6180AR^2 + 6186AS^2 + 6192AT^2 + 6198AU^2 + 6204AV^2 + 6210AW^2 + 6216AX^2 + 6222AY^2 + 6228AZ^2 + 6234AA^2 + 6240AB^2 + 6246AC^2 + 6252AD^2 + 6258AE^2 + 6264AF^2 + 6270AG^2 + 6276AH^2 + 6282AI^2 + 6288AJ^2 + 6294AK^2 + 6300AL^2 + 6306AM^2 + 6312AN^2 + 6318AO^2 + 6324AP^2 + 6330AQ^2 + 6336AR^2 + 6342AS^2 + 6348AT^2 + 6354AU^2 + 6360AV^2 + 6366AW^2 + 6372AX^2 + 6378AY^2 + 6384AZ^2 + 6390AA^2 + 6396AB^2 + 6402AC^2 + 6408AD^2 + 6414AE^2 + 6420AF^2 + 6426AG^2 + 6432AH^2 + 6438AI^2 + 6444AJ^2 + 6450AK^2 + 6456AL^2 + 6462AM^2 + 6468AN^2 + 6474AO^2 + 6480AP^2 + 6486AQ^2 + 6492AR^2 + 6498AS^2 + 6504AT^2 + 6510AU^2 + 6516AV^2 + 6522AW^2 + 6528AX^2 + 6534AY^2 + 6540AZ^2 + 6546AA^2 + 6552AB^2 + 6558AC^2 + 6564AD^2 + 6570AE^2 + 6576AF^2 + 6582AG^2 + 6588AH^2 + 6594AI^2 + 6600AJ^2 + 6606AK^2 + 6612AL^2 + 6618AM^2 + 6624AN^2 + 6630AO^2 + 6636AP^2 + 6642AQ^2 + 6648AR^2 + 6654AS^2 + 6660AT^2 + 6666AU^2 + 6672AV^2 + 6678AW^2 + 6684AX^2 + 6690AY^2 + 6696AZ^2 + 6702AA^2 + 6708AB^2 + 6714AC^2 + 6720AD^2 + 6726AE^2 + 6732AF^2 + 6738AG^2 + 6744AH^2 + 6750AI^2 + 6756AJ^2 + 6762AK^2 + 6768AL^2 + 6774AM^2 + 6780AN^2 + 6786AO^2 + 6792AP^2 + 6798AQ^2 + 6804AR^2 + 6810AS^2 + 6816AT^2 + 6822AU^2 + 6828AV^2 + 6834AW^2 + 6840AX^2 + 6846AY^2 + 6852AZ^2 + 6858AA^2 + 6864AB^2 + 6870AC^2 + 6876AD^2 + 6882AE^2 + 6888AF^2 + 6894AG^2 + 6900AH^2 + 6906AI^2 + 6912AJ^2 + 6918AK^2 + 6924AL^2 + 6930AM^2 + 6936AN^2 + 6942AO^2 + 6948AP^2 + 6954AQ^2 + 6960AR^2 + 6966AS^2 + 6972AT^2 + 6978AU^2 + 6984AV^2 + 6990AW^2 + 6996AX^2 + 7002AY^2 + 7008AZ^2 + 7014AA^2 + 7020AB^2 + 7026AC^2 + 7032AD^2 + 7038AE^2 + 7044AF^2 + 7050AG^2 + 7056AH^2 + 7062AI^2 + 7068AJ^2 + 7074AK^2 + 7080AL^2 + 7086AM^2 + 7092AN^2 + 7098AO^2 + 7104AP^2 + 7110AQ^2 + 7116AR^2 + 7122AS^2 + 7128AT^2 + 7134AU^2 + 7140AV^2 + 7146AW^2 + 7152AX^2 + 7158AY^2 + 7164AZ^2 + 7170AA^2 + 7176AB^2 + 7182AC^2 + 7188AD^2 + 7194AE^2 + 7200AF^2 + 7206AG^2 + 7212AH^2 + 7218AI^2 + 7224AJ^2 + 7230AK^2 + 7236AL^2 + 7242AM^2 + 7248AN^2 + 7254AO^2 + 7260AP^2 + 7266AQ^2 + 7272AR^2 + 7278AS^2 + 7284AT^2 + 7290AU^2 + 7296AV^2 + 7302AW^2 + 7308AX^2 + 7314AY^2 + 7320AZ^2 + 7326AA^2 + 7332AB^2 + 7338AC^2 + 7344AD^2 + 7350AE^2 + 7356AF^2 + 7362AG^2 + 7368AH^2 + 7374AI^2 + 7380AJ^2 + 7386AK^2 + 7392AL^2 + 7398AM^2 + 7404AN^2 + 7410AO^2 + 7416AP^2 + 7422AQ^2 + 7428AR^2 + 7434AS^2 + 7440AT^2 + 7446AU^2 + 7452AV^2 + 7458AW^2 + 7464AX^2 + 7470AY^2 + 7476AZ^2 + 7482AA^2 + 7488AB^2 + 7494AC^2 + 7500AD^2 + 7506AE^2 + 7512AF^2 + 7518AG^2 + 7524AH^2 + 7530AI^2 + 7536AJ^2 + 7542AK^2 + 7548AL^2 + 7554AM^2 + 7560AN^2 + 7566AO^2 + 7572AP^2 + 7578AQ^2 + 7584AR^2 + 7590AS^2 + 7596AT^2 + 7602AU^2 + 7608AV^2 + 7614AW^2 + 7620AX^2 + 7626AY^2 + 7632AZ^2 + 7638AA^2 + 7644AB^2 + 7650AC^2 + 7656AD^2 + 7662AE^2 + 7668AF^2 + 7674AG^2 + 7680AH^2 + 7686AI^2 + 7692AJ^2 + 7698AK^2 + 7704AL^2 + 7710AM^2 + 7716AN^2 + 7722AO^2 + 7728AP^2 + 7734AQ^2 + 7740AR^2 + 7746AS^2 + 7752AT^2 + 7758AU^2 + 7764AV^2 + 7770AW^2 + 7776AX^2 + 7782AY^2 + 7788AZ^2 + 7794AA^2 + 7800AB^2 + 7806AC^2 + 7812AD^2 + 7818AE^2 + 7824AF^2 + 7830AG^2 + 7836AH^2 + 7842AI^2 + 7848AJ^2 + 7854AK^2 + 7860AL^2 + 7866AM^2 + 7872AN^2 + 7878AO^2 + 7884AP^2 + 7890AQ^2 + 7896AR^2 + 7902AS^2 + 7908AT^2 + 7914AU^2 + 7920AV^2 + 7926AW^2 + 7932AX^2 + 7938AY^2 + 7944AZ^2 + 7950AA^2 + 7956AB^2 + 7962AC^2 + 7968AD^2 + 7974AE^2 + 7980AF^2 + 7986AG^2 + 7992AH^2 + 7998AI^2 + 8004AJ^2 + 8010AK^2 + 8016AL^2 + 8022AM^2 + 8028AN^2 + 8034AO^2 + 8040AP^2 + 8046AQ^2 + 8052AR^2 + 8058AS^2 + 8064AT^2 + 8070AU^2 + 8076AV^2 + 8082AW^2 + 8088AX^2 + 8094AY^2 + 8100AZ^2 + 8106AA^2 + 8112AB^2 + 8118AC^2$

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 Since $t + 5$ is odd W is an integer. Then $(1969) = 502 -$
 and $V = W + (t - 1)/2$ are integers. Finally by (9.6) $X = t_0$
 and $V = W + (t - 1)/2$ are integers. Finally by (9.6) $X = t_0$
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